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# STATCOM Control using a PSO-Based IP Controller

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Abstract: This study presents the application of static synchronous compensator (STATCOM) in order to simultaneous voltage support and damping of Low Frequency Oscillations (LFO) at a Single-Machine Infinite-Bus (SMIB) power system installed with STATCOM. PI (Proportional-Integral) type controllers are commonly used controllers for STATCOM control. But due to some drawbacks of PI type controllers, the scope for finding a better control scheme still remains. Concerning this problem, in this study the new IP (Integral-Proportional) type controllers are considered as STATCOM controllers. The parameters of these IP type controllers are tuned using Particle Swarm Optimization (PSO). Also a stabilizer supplementary stabilizer based on STATCOM is incorporated for increasing damping of power system oscillations. To show the ability of IP controllers, this controller is compared with classical PI type controllers. Simulation results emphasis on the better performance of IP controller in comparison with PI controller.

Key words: IP controller, low frequency oscillations, particle swarm optimization, static synchronous compensator, voltage control

# INTRODUCTION

The rapid development of the high-power electronics industry has made Flexible AC Transmission System (FACTS) devices viable and attractive for utility applications. FACTS devices have been shown to be effective in controlling power flow and damping power system oscillations. In recent years, new types of FACTS devices have been investigated that may be used to increase power system operation flexibility and controllability, to enhance system stability and to achieve better utilization of existing power systems (Hingorani et al., 2000). The static synchronous compensator (STATCOM) is one of the most important FACTS devices and it is based on the principle that a voltagesource inverter generates a controllable AC voltage source behind a transformer-leakage reactance so that the voltage difference across the reactance produces active and reactive power exchange between the STATCOM and the transmission network. The STATCOM is one of the important 'FACTS' devices and can be used for dynamic compensation of power systems to provide voltage support and stability improvement (Gyugyi et al., 1990; Gyugyi, 1979; Schauder et al., 1993; Schauder et al., 1995; Ekanayake et al., 1995; Saad-Saoud et al., 1998; Trainner et al., 1994; Ainsworth et al., 1998; Mori et al., 1993). In Wang et al. (1999) a unified Phillips-Heffron model (Heffron et al., 1952) of power systems installed with a STATCOM is established. Also STATCOM can be used for transient stability improvement by damping of low frequency power system oscillations (Tambey et al.,

2003; Cheng et al., 1986; Al-Awami et al., 2007; Mishra et al., 2000; Eldamaty et al., 2005).

The objective of this study is to investigate the ability of STATCOM for voltage support and damping of power system oscillations at the same time. In this paper the STATCOM internal controllers (bus-voltage controller and DC link voltage regulator) are considered as IP type controllers. PSO is handled for tuning the parameters of these IP type controllers. Also a supplementary stabilizer based on STATCOM is considered for damping of power system oscillations and stability enhancement. Different loading conditions are considered to show ability of STATCOM and also comparing IP and PI type controllers. Simulation results show the effectiveness of STATCOM in power system stability and control by using the new IP type controller.

# METHODOLOGY

**Illustrative test:** Figure 1 shows the case study system in this paper. The system is a Single Machine Infinite Bus (SMIB) power system with STATCOM installed.

**Nonlinear model of the system:** A non-linear dynamic model of the system is derived by disregarding the resistances of all components of the system (generator, transformer, transmission line and shunt converter transformer) and the transients of the transmission lines and transformer of the STATCOM. The nonlinear dynamic model is given as (1) (Wang *et al.*, 1999):

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Fig. 1: A single-machine infinite-bus power system installed with STATCOM



Fig. 2: Transfer function model of the system including STATCOM

$$\begin{cases} \dot{\omega} = (P_m - P_e - D\omega) / M \\ \dot{\delta} = \omega_0 (\omega - 1) \\ \dot{E}'_q = (-E_q + E_{fd}) / T'_{do} \\ \dot{E}'_{fd} = (-E_{fd} + K_a (V_{ref} - V_t)) / T_a \\ \dot{V}_{dc} = \frac{3m_E}{4C_{dc}} (\sin(\delta_E) I_{Ed} + \cos(\delta_E) I_{Eq}) \end{cases}$$
(1)

**Linear model:** A linear dynamic model is obtained by linearising the non-linear model around the nominal operating condition. The linearised model is given as (2):

$$\begin{cases} \Delta \hat{\delta} = w_0 \Delta w \\ \Delta \dot{\omega} = (-\Delta P_e - D\Delta \omega) / M \\ \Delta \dot{E}'_q = (-\Delta E_q + \Delta E_{fd}) / T'_{do} \\ \Delta \dot{E}_{fd} = -(1/T_A) \Delta E_{fd} - (K_A / T_A) \Delta V_i \\ \Delta \dot{v}_{dc} = K_7 \Delta \delta + K_8 \Delta E'_q - K_9 \Delta v_{dc} + K_{ce} \Delta m_E \\ + K_{coc} \Delta \delta_E \end{cases}$$

$$(2)$$

where,

$$\begin{split} \Delta P_{e} &= K_{1}\Delta\delta + K_{2}\Delta E_{q}^{\prime} + K_{pd}\Delta v_{dc} + K_{pe}\Delta m_{E} + K_{p\delta E}\Delta\delta_{E} \\ \Delta E_{q} &= K_{4}\Delta\delta + K_{3}\Delta E_{q}^{\prime} + K_{qd}\Delta v_{dc} + K_{qe}\Delta m_{E} + K_{q\delta E}\Delta\delta_{E} \\ \Delta V_{t} &= K_{5}\Delta\delta + K_{6}\Delta E_{q}^{\prime} + K_{vd}\Delta v_{dc} + K_{ve}\Delta m_{E} + K_{v\delta E}\Delta\delta_{E} \end{split}$$

Figure 2 shows the transfer function model of the system including STATCOM. The model has constant parameters which are denoted by  $K_{ij}$ . These constant parameters are function of the system parameters and the initial operating condition. The control vector U in Fig. 2 is defined as (3):

$$U = [\Delta m_E \ \Delta \delta_E]^T \tag{3}$$

where,

- $\Delta m_{E} \quad : \quad Deviation \ in pulse \ width \ modulation \ index \ m_{E} \\ of \ shunt \ inverter. \ By \ controlling \ m_{E}, \ the \ output \ voltage \ of \ the \ shunt \ converter \ is \ controlled$
- $\Delta d_E$ : Deviation in phase angle of the shunt inverter voltage. By controlling  $\delta_E$ , exchanging active power between the STATCOM and the power system is controlled

It should be noted that  $K_{pu}$ ,  $K_{qu}$ ,  $K_{vu}$  and  $K_{cu}$  in Fig. 2 are the row vectors and defined as follows:

$$\begin{split} K_{pu} &= [K_{pe} \quad K_{p\tilde{\&}}]; \ K_{qu} = [K_{qe} \quad K_{q\tilde{\&}}] \\ K_{vu} &= [K_{ve} \quad K_{v\tilde{\&}}]; \ K_{cu} = [K_{ce} \quad K_{c\tilde{\&}}] \end{split}$$

The dynamic model of the system in state-space form is obtained as (4). The typical values of system parameters for the nominal operating condition are given in Appendix.

$$\begin{bmatrix} \Delta \dot{\delta} \\ \Delta \dot{w} \\ \Delta \dot{E}_{q}' \\ \Delta \dot{E}_{fd} \\ \Delta \dot{v}_{dc} \end{bmatrix} = \begin{bmatrix} 0 & w_{0} & 0 & 0 & 0 \\ -\frac{K_{1}}{M} & 0 & -\frac{K_{2}}{M} & 0 & -\frac{K_{pd}}{M} \\ -\frac{K_{4}}{M} & 0 & \frac{K_{3}}{T_{do}'} & -\frac{1}{T_{do}'} & -\frac{K_{qp}}{T_{do}'} \\ -\frac{K_{4}K_{5}}{T_{A}} & 0 & -\frac{K_{4}K_{6}}{T_{A}} & -\frac{1}{T_{A}} & \frac{K_{A}K_{vd}}{T_{A}} \\ K_{7} & 0 & K_{8} & 0 & -K_{9} \end{bmatrix}$$

$$\times \begin{bmatrix} \Delta \delta \\ \Delta w \\ \Delta E_{q}' \\ \Delta E_{fd}' \\ \Delta V_{dc} \end{bmatrix} + \begin{bmatrix} 0 & 0 \\ -\frac{K_{pe}}{M} & -\frac{K_{p\dot{w}}}{T_{do}'} \\ -\frac{K_{qe}}{T_{A}'} & -\frac{K_{q\dot{w}}}{T_{do}'} \\ -\frac{K_{A}K_{ve}}{T_{A}} & -\frac{K_{A}K_{v\dot{w}}}{T_{A}} \\ Kce & K_{c\dot{w}} \end{bmatrix} \times \begin{bmatrix} \Delta m_{E} \\ \Delta \delta_{E} \end{bmatrix}$$

$$(4)$$

**IP controller:** As referred before, in this study IP type controllers are considered as STATCOM internal



Fig. 3: Structure of the IP controller



Fig. 4: Output of IP and PI regulators with the same damping coefficient and the same band width at the same step input signal command (Sul, 2011)



Fig. 5: DC-voltage regulator

controllers. Figure 3 shows the structure of IP controller. It has some clear differences with PI controller. In the case of IP regulator, at the step input, the output of the regulator varies slowly and its magnitude is smaller than the magnitude of PI regulator at the same step input (Sul, 2011). Also as shown in Fig. 4, If the outputs of the both regulators are limited as the same value by physical constraints, then compared to the bandwidth of PI regulator the bandwidth of IP regulator can be extended without the saturation of the regulator output (Sul, 2011).

**STATCOM controllers:** In this study three control strategies are considered for STATCOM:

- Bus voltage controller
- DC voltage regulator
- Power system oscillation-damping controller

**Internal STATCOM controllers:** STATCOM has two internal controllers which are Bus voltage controller and DC voltage regulator. In order to control of DC voltage, a DC-voltage regulator is incorporated. DC-voltage is



Fig 6. Generator terminals voltage controller



Fig 7. Stabilizer controller

Table 1: E	Eigen-values of the closed-loop system	
-17.1146,	+0.0213±3.711i, -0.5401±0.4991i	

regulated by modulating the phase angle of the shunt converter voltage. Figure 5 shows the structure of the DCvoltage regulator. Also Fig. 6 shows the structure of the generator terminals voltage controller. The generator terminals voltage controller regulates the voltage of generator terminals during post fault in the system.

**Power system oscillations-damping controller:** A stabilizer controller is provided to improve damping of power system oscillations and stability enhancement. This controller is considered as a lead-lag compensator. This stabilizer provides an electrical torque in phase with the speed deviation in order to improve damping of power system oscillations. The transfer function model of the stabilizer controller is shown in Fig. 7.

**Analysis:** For the nominal operating condition the eigenvalues of the system are obtained using state-space model of the system presented in (4) and these eigen-values are listed in Table 1. It is seen that the system is unstable and needs to power system stabilizer (damping controller) for stability.

**Design of damping controller for stability:** The damping controllers are designed to produce an electrical torque in phase with the speed deviation according to phase compensation method. The two control parameters of the STATCOM ( $m_E$  and  $\delta_E$ ) can be modulated in order to produce the damping torque. In this study  $m_E$  is modulated in order to damping controller design also the speed deviation  $\omega$  is considered as the input to the damping controllers. The structure of damping controller has been shown in Fig. 7. It consists of gain, signal

Table 2:	Eigen-values	of	the	closed-loop	system	n with stabilizer
	controller					
-18,4188	12.31555.	881	2.	-0.9251±0.	9653.	-0.8211±0.7903

washout and phase compensator block. The parameters of the damping controller are obtained using the phase compensation technique. The detailed step-by-step procedure for computing the parameters of the damping controllers using phase compensation technique is presented by Kundur (1993). Damping controller has been designed and obtained as (5):

Damping controlle = 
$$\frac{481.3021 \ s \ (s+4.712)}{(s+0.1) \ (s+5.225)}$$
 (5)

The eigen-values of the system with stabilizer controller are listed in Table 2 and it is clearly seen that the system is stable.

**Internal STATCOM controllers design:** After system stabilizing, the next step is to design the internal STATCOM controllers (DC voltage regulator and generator terminals voltage controller). As mentioned before, IP type controllers are considered for STATCOM and these controllers are tuned using PSO. In the next section an introduction about PSO is presented.

**Particle swarm optimization:** PSO was formulated by Edward and Kennedy (1995). The thought process behind the algorithm was inspired by the social behavior of animals, such as bird flocking or fish schooling. PSO begins with a random population matrix. It has no evolution operators such as crossover and mutation. The rows in the matrix are called particles. They contain the variable values and are not binary encoded. Each particle moves about the cost surface with a velocity. The particles update their velocities and positions based on the local and global best solutions as shown in (6) and (7):

$$V_{m,n}^{new} = w \times V_{m,n}^{old} + \Gamma_1 \times r_1 \times (P_{m,n}^{localbast} - P_{m,n}^{old}) + \Gamma_2 \times r_2 \times (P_{m,n}^{globalbast} - P_{m,n}^{old})$$
(6)

$$P_{m,n}^{new} = P_{m,n}^{old} + \Gamma V_{m,n}^{new} \tag{7}$$

where,  $V_{m,n}$ : Particle velocity;  $P_{m,n}$ : Particle variables; W: Inertia weight;  $r_1$ ,  $r_2$ : Independent uniform random numbers;  $\Gamma_1$ ,  $\Gamma_2$ : Learning factors; Plocal bem,  $n P_{m,n}^{localbest}$ . Best global solution;  $P_{m,n}^{global best}$ : Best global solution.

The PSO algorithm updates the velocity vector for each particle then adds that velocity to the particle position or values. Velocity updates are influenced by both the best global solution associated with the lowest cost ever found by a particle and the best local solution

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Table 3: Optimum values of IP typ	e controllers	
IP controller of DC voltage	K <sub>DP</sub>	9.6712
IP controller of hus voltage	K K	25.00
	K <sub>VP</sub> K <sub>VI</sub>	31.821
Table 4: Optimum values of PI typ	e controller	
PI controller of DC voltage	K <sub>DP</sub>	2.066
-	K <sub>DI</sub>	1.101
PI controller of bus voltage	K <sub>VP</sub>	0.3201
-	Kvi	33.812

associated with the lowest cost in the present population. If the best local solution has a cost less than the cost of the current global solution, then the best local solution replaces the best global solution. The particle velocity is reminiscent of local minimizes that use derivative information, because velocity is the derivative of position. The advantages of PSO are that it is easy to implement and there are few parameters to adjust. The PSO is able to tackle tough cost functions with many local minima (Randy and Sue, 2004).

**Controllers adjustment using PSO:** In this section the parameters of the proposed IP type controllers are tuned using PSO. All two IP controllers are simultaneously tuned using PSO. In this study the performance index is considered as (8). In fact, the performance index is the Integral of the Time multiplied Absolute value of the Error (ITAE):

$$ITAE = \int_{0}^{t} t \left| \Delta \omega \right| dt + \int_{0}^{t} t \left| \Delta V_{DC} \right| dt + \int_{0}^{t} t \left| \Delta V_{t} \right| dt \quad (8)$$

where,  $\Delta w$  is the frequency deviation,  $\Delta_{\text{VDC}}$  is the deviation of DC voltage,  $\Delta V_t$  is the deviation of bus voltage and parameter "t" in ITAE is the simulation time. It is clear to understand that the controller with lower ITAE is better than the other controllers. To compute the optimum parameter values, a 0.1 step change in mechanical torque ( $\Delta$ Tm) is assumed and the performance index is minimized using PSO. In order to acquire better performance, number of particle, particle size, number of iteration,  $\Gamma_1$ ,  $\Gamma_2$  and  $\Gamma$  are chosen as 12, 4, 50, 2, 2 and 1, respectively. Also, the inertia weight, w, is linearly decreasing from 0.9 to 0.4. It should be noted that PSO algorithm is run several times and then optimal set of parameters is selected The optimum values resulting from minimizing the performance index are presented in Table 3. In order to show effectiveness of IP method, the classical PI type controllers are also considered for STATCOM control and the parameters of these PI type controllers are tuned using PSO. The results are listed in Table 4.

## **RESULTS AND DISCUSSION**

In order to evaluate the effectiveness of STATCOM and also comparing IP and PI type controllers, two

Table 5: The calculated ITAE index for the both controllers

	IP	PI
Nominal operating condition	0.0102	0.0396
Heavy operating condition	0.0119	0.0419

Fable 6 <sup>.</sup> The calculated	control effort signal	for the both controllers
able 0. The calculated	control choit signal	for the both controllers

	IP	PI
Nominal operating condition	2.041	2.0711
Heavy operating condition	2.162	2.1741



Fig. 8: Dynamic response  $DV_{DC}$  following 5% step change in the reference mechanical torque; Solid (IP controller); Dashed (PI controller)

operating conditions are considered as nominal and heavy operating conditions. The parameters for these two operating conditions are presented in the Appendix. It should be note that IP and PI controllers have been designed for the nominal operating condition. In order to demonstrate the robustness performance of the proposed methods, The ITAE is calculated following 5% step change in the reference mechanical torque ( $\Delta$ Tm) at all operating conditions (Nominal and Heavy) and results are shown at Table 5. Following step change, the IP controller has better performance than PI at all operating conditions. The other important factor in the comparison of controllers is control effort signal. In this study following index is considered to compare of the IP and PI controllers.

Control effort = 
$$\int_{0}^{t} t |\Delta u| dt$$
 (9)

where, u shows the control effort signal. The proposed metric is calculated for the both PI and IP controllers. The results are listed in Table 6. The results show that the IP controller injects a lower control signal. Thus, in the case of IP controller, it is less probable to saturation of control signal.

Also simulation results following 0.05 step change in reference mechanical torque ( $\Delta$ Tm) in the heavy operating condition are shown in Fig. 8-10. Each figure contains to plots as solid for IP controller and dashed for PI controller. Figure 8 shows that the DC voltage of STATCOM goes back to zero after disturbances and the steady state error has been removed and Fig. 9 shows the



Fig. 9: Dynamic response DV<sub>1</sub> following 5% step change in the reference mechanical torque; Solid (IP controller); Dashed (PI controller)



Fig. 10: Dynamic response  $\Delta \omega$  following 5% step change in the reference mechanical torque; Solid (IP controller); Dashed (PI controller)

# CONCLUSION

In this study STATCOM successfully incorporated in order to simultaneous control of bus voltage and DC voltage of generator's bus which is driven back to zero after oscillations. The results show that STATCOM can simultaneously control bus voltage and DC voltage. Figure 10 shows the deviation of synchronous speed and it is seen that the supplementary stabilizer greatly enhances the damping of the power system oscillations and thus the system becomes more stable and robust. In all cases, the IP method has better performance than PI in control of power system and also stability enhancement. voltage. Also a supplementary stabilizer based STATCOM incorporated for damping power system oscillations and stability enhancement. Internal STATCOM controllers modeled as IP type and their parameters tuned using PSO. The simulation results showed that the STATCOM with IP controllers has better performance in control and stability than STATCOM with PI controllers. The multi objective abilities of STATCOM in control and stability successfully were showed by time domain simulations.

**Appendix**: The nominal system parameters are listed in Table 7. Also the system operating conditions are defined as Table 8 (Operating condition 1 is the nominal operating condition).

Table 7: System parameters					
Generator	M = 8 Mj/MVA	$T'_{do} = 5.044 \text{ s}$	$X_{d} = 1 \text{ p.u.}$		
	$X_{a} = 0.6 \text{ p.u.}$	X'd = 0.3 p.u.	$\mathbf{D} = 0$		
Excitation system	-	$K_a = 10$	$T_a = 0.05 \text{ s}$		
Transformers		$X_{te} = 0.1 \text{ p.u.}$	$X_{SDT} = 0.1 \text{ p.u.}$		
Transmission lines		$X_{T1} = 1 \text{ p.u.}$	$X_{T2} = 1.25$ p.u.		
DC link parameters		$V_{DC} = 2 p.u.$	$C_{DC} = 3 \text{ p.u.}$		
STATCOM parameter	ers	$M_e = 1.0224$	$\delta_{\rm E} = 22.24^{\circ}$		

Table 8: System operati	ng conditions		
Operating condition 1	P = 1 p.u.	Q = 0.2 p.u.	$V_t = 1.03 \text{ p.u.}$
Operating condition 2	P = 1.08  p.u.	Q = 0.25  p.u.	$V_t = 1.03 \text{ p.u.}$

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